

Connected Masses

Strategies to solve problems

(A) Draw a FBD for each mass.

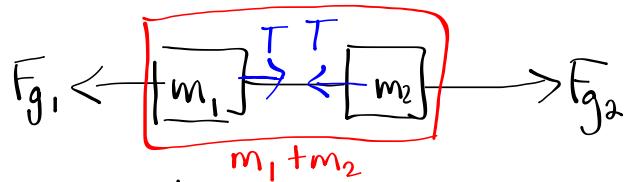
Assign + to the direction each mass moves

Set up $F_{\text{net}} = ma$

Usually you end up solving for a and T

(B) "Stretch" out the masses so the system lies horizontally

$\rightarrow +$



Tug-o-war between F_{g2} and F_{g1}

$$F_{\text{net}} = F_{g2} - F_{g1}$$

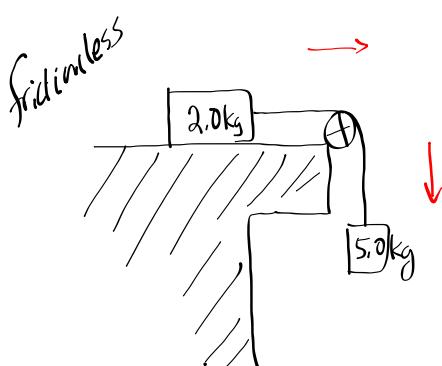
↑
this F_{net} acts on $m_1 + m_2$

find acceleration

Draw a FBD for either m_1 or m_2 in order to find the tension

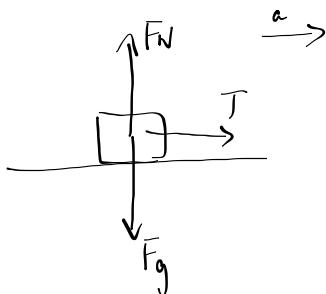
NOTE: Max acceleration is 9.8 m/s^2

Example (FOP | 159)



What is the acceleration
and the tension in
the string?

Consider the 2.0kg mass:



$$\vec{F}_{\text{net}} = m\vec{a}$$

$$T = (2.0\text{kg})a$$

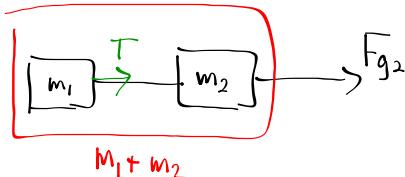
Consider the 5.0kg mass:

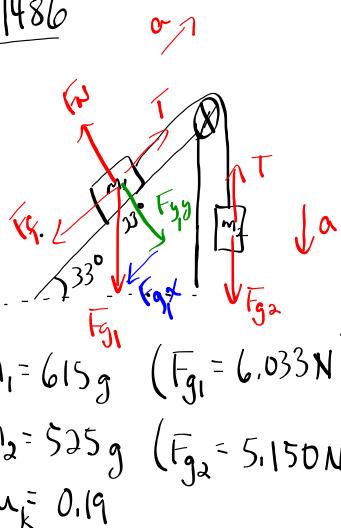
$$\begin{aligned} & \vec{F}_{\text{net}} = m\vec{a} \\ & F_{g_2} - T = m_2 a \\ & 49.05\text{N} - T = (5.0\text{kg})a \\ & 49.05 - 2.0a = 5.0a \\ & 49.05 = 7.0a \\ & a = 7.0\text{m/s}^2 \end{aligned}$$

Sub $a = 7.0\text{m/s}^2$ into:

$$\begin{aligned} T &= (2.0\text{kg})a \\ T &= (2.0\text{kg})(7.0\text{m/s}^2) \\ T &= 14\text{N} \end{aligned}$$

or
the other
way



MP|486

$$m_1 = 615 \text{ g} \quad (F_{g1} = 6.033 \text{ N})$$

$$m_2 = 525 \text{ g} \quad (F_{g2} = 5.150 \text{ N})$$

$$\mu_k = 0.19$$

find acc + tension

The biggest value that T can be is F_{g2} (5.150 N) if the block m_1 goes uphill and m_2 goes down.

So we need to see if $(F_{g2}) T_{\max} > F_f + F_{gx}$. If it is, then m_1 will go uphill and m_2 will go straight down.

$$T_{\max} = F_{g2} = 5.150 \text{ N}$$

$$F_{gx} = F_g \sin \theta = (6.033 \text{ N}) \sin 33^\circ = 3.286 \text{ N}$$

$$F_f = \mu F_N = \mu F_{gy} = \mu F_g \cos \theta = (0.19)(6.033 \text{ N})(0.633) \\ = 0.961 \text{ N}$$

$$4.247 \text{ N}$$

Since the maximum tension ($= F_{g2}$)

is greater than $F_{gx} + F_f$, then m_1 will go uphill and m_2 will go down.

Consider m_1 only

$$\vec{F}_{\text{net}} = m \vec{a}$$

$$T - (F_{gx} + F_f) = m_1 a$$

$$T - 4.247 \text{ N} = (0.615 \text{ kg}) a$$

Consider m_2 only

$$\vec{F}_{\text{net}} = m \vec{a}$$

$$F_{g2} - T = m_2 a$$

$$5.150 \text{ N} - T = (0.525 \text{ kg}) a$$

↓
finish → find a and T

To Do

① PP|478 (elevator)

prob → ② PP|485 (Atwood's)

③ PP|488-489 (horizontal + inclines)